

**LEARNING OBJECTIVE:** We will multiply polynomials. (Alg1M1L4)

**CONCEPT DEVELOPMENT:**

We can use ARRAY MODELS to MULTIPLY polynomials.

$$(x - 1)(x^3 + 6x^2 - 5)$$

	$x^3$	$6x^2$	$-5$
$x$	$x^4$	$6x^3$	$-5x$
$-1$	$-x^3$	$-6x^2$	$5$

$$x^4 + 5x^3 - 6x^2 - 5x + 5$$

4<sup>th</sup> degree, 5 terms.

Multiplying polynomials requires us to apply the DISTRIBUTIVE PROPERTY.

$$(x - 1)(x^3 + 6x^2 - 5)$$

$$\text{Distrib. A } [(x-1)(x^3)] + [(x-1)(6x^2)] - [(x-1)(5)]$$

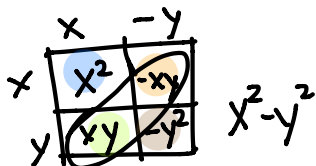
$$\text{Distrib. B } x(x^3 + 6x^2 - 5) - 1(x^3 + 6x^2 - 5)$$

When you multiply polynomials,  
think **ARRAY MODELS**  
think **DISTRIBUTIVE PROPERTY !!**

### Special Products of Binomials

#### Sum and Difference

$$(x + y)(x - y)$$

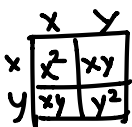


$$x^2 - y^2 \leftarrow \text{Difference of 2 squares}$$

#### Square of a binomial

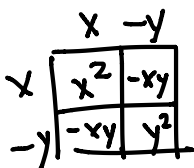
$$(x + y)^2$$

$$(x + y)(x + y)$$



$$x^2 + 2xy + y^2$$

$$(x - y)^2$$



$$x^2 - 2xy + y^2$$

**Factoring:** the process of extracting common terms from a polynomial. It is the complement to applying the distributive property.

*Example:* Given the expression  $6a + 14a^2$  we can extract  $2a$  from each term to create a new expression using the distributive property:  $2a(3 + 7a)$ .

*Quick Practice:*

$$2x^4 + 2x^5 + 2x^6 = 2x^4(1 + x + x^2)$$

$$\frac{2x^{10} + 2x^5 + 2x^4}{x^6 + x + 1} = 2x^4$$

$$6z^2 - 15z = 3z(2z - 5)$$

$$\sqrt{42w^3 - 14w + 77w^5} = 7w(\dots)$$

$$\sqrt{\frac{3}{2}s^2 + \frac{1}{2}} = \frac{1}{2}(3s^2 + 1)$$

$$\sqrt{(4x + 3)(x^2 + x^3) - (2x - 2)(x^2 + x^3)}$$

$$(x^2 + x^3)(4x + 3 - 2x + 2)$$

$$(x^2 + x^3)(2x + 5)$$

**GUIDED PRACTICE:**

**Steps for Multiplying Polynomials**

1. Distribute each term in the first polynomial to each term in the second polynomial.
2. Simplify as needed.

<p>2 MONOMIALS</p> $\boxed{4x^2(3x^4y^3)}$ $(4 \cdot 3)(x^2 \cdot x^4)y^3$ $12x^6y^3$ $12x^6y^3$	$-2x^4y^5(6xy^3)$ $\boxed{-12x^5y^8}$									
<p><i>Monomial x polynomial</i></p> $5k(2k^2 - 5k + 3)$ <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding: 0 10px;"><math>2k^2</math></td> <td style="padding: 0 10px;"><math>-5k</math></td> <td style="padding: 0 10px;"><math>3</math></td> </tr> <tr> <td style="padding: 0 10px;"><math>5k</math></td> <td style="padding: 0 10px;"><math>10k^3</math></td> <td style="padding: 0 10px;"><math>-25k^2</math></td> </tr> <tr> <td></td> <td style="padding: 0 10px;"><math>15k</math></td> <td></td> </tr> </table> $10k^3 - 25k^2 + 15k$	$2k^2$	$-5k$	$3$	$5k$	$10k^3$	$-25k^2$		$15k$		$8t(3s^3 + 4s^2t - 2t)$ <div style="text-align: right;">✓</div>
$2k^2$	$-5k$	$3$								
$5k$	$10k^3$	$-25k^2$								
	$15k$									
<p>Binomial x Binomial</p> $(x^2 + 3)(x + 2)$ <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding: 0 10px;"><math>x^2</math></td> <td style="padding: 0 10px;"><math>x</math></td> <td style="padding: 0 10px;"><math>2</math></td> </tr> <tr> <td style="padding: 0 10px;"><math>x^2</math></td> <td style="padding: 0 10px;"><math>x^3</math></td> <td style="padding: 0 10px;"><math>2x^2</math></td> </tr> <tr> <td style="padding: 0 10px;"><math>3</math></td> <td style="padding: 0 10px;"><math>3x</math></td> <td style="padding: 0 10px;"><math>6</math></td> </tr> </table> $x^3 + 2x^2 + 3x + 6$	$x^2$	$x$	$2$	$x^2$	$x^3$	$2x^2$	$3$	$3x$	$6$	$(x - 4)(x^2 - 3)$ $x^3 - 4x^2 - 3x + 12$ <div style="text-align: right;">✓</div>
$x^2$	$x$	$2$								
$x^2$	$x^3$	$2x^2$								
$3$	$3x$	$6$								

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Math 7.2, Period \_\_\_\_\_

Mr. Rogove

Date: \_\_\_\_\_

<p><math>(3x + 2)(-2x^3 + 5x - 6)</math></p> <table border="1" style="margin-left: 40px;"> <tr> <td></td> <td><math>-2x^3</math></td> <td><math>5x</math></td> <td><math>-6</math></td> </tr> <tr> <td><math>3x</math></td> <td><math>-6x^4</math></td> <td><math>15x^2</math></td> <td><math>-18x</math></td> </tr> <tr> <td><math>2</math></td> <td><math>-4x^3</math></td> <td><math>10x</math></td> <td><math>-12</math></td> </tr> </table> <p><math>(3x \cdot -2x^3) + (3x \cdot 5x) + (3x \cdot -6)</math>  <math>2L</math></p>		$-2x^3$	$5x$	$-6$	$3x$	$-6x^4$	$15x^2$	$-18x$	$2$	$-4x^3$	$10x$	$-12$	<p><math>(3x + 1)(x^3 + 4x^2 - 7)</math></p>
	$-2x^3$	$5x$	$-6$										
$3x$	$-6x^4$	$15x^2$	$-18x$										
$2$	$-4x^3$	$10x$	$-12$										
<p><math>(10x + 7)^2</math></p>	<p><math>(\frac{1}{2}x + 4)^2</math></p> <table border="1" style="margin-left: 40px;"> <tr> <td></td> <td><math>\frac{1}{2}x</math></td> <td><math>4</math></td> </tr> <tr> <td><math>\frac{1}{2}x</math></td> <td><math>\frac{1}{4}x^2</math></td> <td><math>2x</math></td> </tr> <tr> <td><math>4</math></td> <td><math>2x</math></td> <td><math>16</math></td> </tr> </table> <p><math>\frac{1}{4}x^2 + 4x + 16</math></p> <p><math>(\frac{1}{2}x)^2 + 2(\frac{1}{2}x)(4) + 4^2</math>  <math>\frac{1}{4}x^2 + 4x + 16</math></p>		$\frac{1}{2}x$	$4$	$\frac{1}{2}x$	$\frac{1}{4}x^2$	$2x$	$4$	$2x$	$16$			
	$\frac{1}{2}x$	$4$											
$\frac{1}{2}x$	$\frac{1}{4}x^2$	$2x$											
$4$	$2x$	$16$											
<p><math>(2x + 6)(2x - 6)</math></p>	<p><math>(3x - 5)(3x + 5)</math></p> <table border="1" style="margin-left: 40px;"> <tr> <td></td> <td><math>3x</math></td> <td><math>-5</math></td> </tr> <tr> <td><math>3x</math></td> <td><math>9x^2</math></td> <td><math>-15x</math></td> </tr> <tr> <td><math>5</math></td> <td><math>15x</math></td> <td><math>-25</math></td> </tr> </table> <p><math>9x^2 - 25</math></p>		$3x$	$-5$	$3x$	$9x^2$	$-15x$	$5$	$15x$	$-25$			
	$3x$	$-5$											
$3x$	$9x^2$	$-15x$											
$5$	$15x$	$-25$											

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**INDEPENDENT PRACTICE:**

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**ACTIVATING PRIOR KNOWLEDGE:**

We can use the distributive property:

$\begin{array}{l} 5(3x^3 - 11y^2) \\ (5 \cdot 3x^3) - (5 \cdot 11y^2) \\ 15x^3 - 55y^2 \end{array}$	$\begin{array}{l} 12(4a^2b - 9c^5) \\ (12 \cdot 4a^2b) - (12 \cdot 9c^5) \\ 48a^2b - 108c^5 \end{array}$
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**CLOSURE:**

Is the product of 2 polynomials ALWAYS a polynomial?

**NOTES:**

This is Go Math Pilot, mapping to lesson 14-3. In ENY, this translates to lesson 9 of Alg 1, module 1.

Homework from Textbook Page 507-08 Questions 10-27.