

NAME: _____

Math _____, Period _____

Mr. Rogove

Date: _____

LEARNING OBJECTIVE: We will compare numbers written in scientific notation. (G8M1L11)

ACTIVATING PRIOR KNOWLEDGE:

What number is bigger?

$99,999,999$ or $111,111,111$ 8 digits 9 digits	$1,000,100$ or $889,999$ 1.0001×10^6 v. 8.89999×10^5
$328,000921$ or 328.01 hundredth 9 tenths, 9 hundredths	0.0009 or 0.001 9×10^{-4} 1×10^{-3}
9.76×10^7 or 1.01×10^8 $8 > 7$ (Magnitude)	7.91×10^{-1} or 7.911×10^{-2} $-1 > -2$

CONCEPT DEVELOPMENT:

Comparing Numbers

If two whole numbers have different numbers of digits, the number with more digits is greater.

Given two numbers in scientific notation:

$a \times 10^m$ and $b \times 10^n$, if $m < n$, then $a \times 10^m < b \times 10^n$.

Examples:

$9.99 \times 10^{17} < 1.111 \times 10^{18}$ because $17 < 18$.

$4.5454 \times 10^{-34} < 4.5555 \times 10^{-31}$ because $-34 < -31$

Compare the following:

<p>① 9.9×10^7 and 1.001×10^9</p> <p>9.9×10^7 1.001×10^9</p>	<p>② 873×10^5 and 8.72×10^7</p> <p><u>Not Sci. Not.</u></p> <p>$8.73 \times 10^7 > 8.72 \times 10^7$</p>
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GUIDED PRACTICE:

Steps for Comparing Numbers Written in Scientific Notation

1. Read the description of the numbers carefully.
2. Express both numbers as a product with the same power of 10.
3. Look at the values of the products not raised to the power of 10 and compare them.

<p>Among the closest galaxies to Earth, <i>M82</i> is about 1.15×10^7 light-years away and <i>Leo I Dwarf</i> is about 8.2×10^5 light-years away. Which is closer?</p> <p><i>Leo is closer than M82</i></p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;"><i>M82</i></td> <td style="text-align: center;">1.15×10^7</td> </tr> <tr> <td style="text-align: center;"><i>Leo I</i></td> <td style="text-align: center;">8.2×10^5</td> </tr> </table>	<i>M82</i>	1.15×10^7	<i>Leo I</i>	8.2×10^5	<p>The Fornax Dwarf galaxy is 4.6×10^5 light-years away from Earth, while Andromeda I is 2.43×10^6 light-years away from Earth. Which is closer?</p> <p><i>Fornax Dwarf is closer.</i></p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;">$\frac{2.43}{4.6}$</td> <td style="text-align: center;">$\frac{10^6}{10^5}$</td> <td style="text-align: center;"><i>About 5x closer</i></td> </tr> </table>	$\frac{2.43}{4.6}$	$\frac{10^6}{10^5}$	<i>About 5x closer</i>			
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<p>The average lifespan of the <u>tau lepton</u> is 2.906×10^{-13} seconds and the average lifespan of the <u>neutral pion</u> is 8.4×10^{-17} seconds. Explain which subatomic particle has the longer lifespan.</p> <p><i>Tau lepton longer lifespan.</i></p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;">2.906×10^{-13}</td> <td style="text-align: center;">8.4×10^{-17}</td> </tr> </table>	2.906×10^{-13}	8.4×10^{-17}	<p>The wavelength of the color red is about 6.5×10^{-9} meters long. The wavelength of the color blue is about 4.75×10^{-9} meters long. Which wavelength is longer? <i>Longer means bigger number.</i></p> <p style="text-align: center;">$4.75 \times 10^{-9} < 6.5 \times 10^{-9}$</p> <p style="text-align: center;"><i>BLUE < RED</i></p>								
2.906×10^{-13}	8.4×10^{-17}										
<p>Which is larger: 9.3×10^{28} or 9.2879×10^{28}</p>	<p>Which is larger: 5.3×10^{421} or 5.301×10^{421}</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: right;">5.301×10^{421}</td> <td></td> </tr> <tr> <td style="text-align: right;">$- 5.3 \times 10^{421}$</td> <td></td> </tr> <tr> <td style="text-align: right;"><hr/></td> <td></td> </tr> <tr> <td style="text-align: right;">0.001×10^{421}</td> <td></td> </tr> <tr> <td style="text-align: right;">1×10^{418}</td> <td></td> </tr> </table>	5.301×10^{421}		$- 5.3 \times 10^{421}$		<hr/>		0.001×10^{421}		1×10^{418}	
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2.43×10^6
 4.6×10^5
 $\frac{2.43 \times 10^6}{4.6 \times 10^5}$
 19.7×10^0

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INDEPENDENT PRACTICE:

Compare the two numbers.

The mass of a neutron is approximately 1.674927×10^{-27} kg. The mass of a proton is 1.672622×10^{-27} kg. Explain which is heavier?

$4 > 2$

NEUTRON

The average lifespan of the Z boson is approximately 3×10^{-25} seconds and the average lifetime of a neutral rho meson is approximately 4.5×10^{-24} seconds.

Which has a longer lifetime?

Approximately how many times longer is the lifespan of the longer living subatomic particle?

Rho Meson

by $\frac{4.5 \times 10^{-24}}{3 \times 10^{-25}} = 1.5 \times 10$
15 times

* Gross Domestic Product (GDP) is an economic measurement used to show the market value of all the goods and services from a country. Below are the GDP figures for 8 countries for 2012 according to the United Nations. **Arrange them in order from greatest to least.**

	Country	2012 GDP (in dollars)
2	China	8.3584×10^{12}
6	Italy	2.013392×10^{12}
7	Spain	1.322126×10^{12}
1	United States	1.62446×10^{13}
4	Brazil	2.254109×10^{12}
5	Russia	2.029812×10^{12}
8	Turkey	7.88299×10^{11}
3	France	2.611221×10^{12}

Approximately how many times larger is the largest economy on this list compared to the smallest (you can round to the nearest tenth before doing any calculations)?

$\frac{\text{USA}}{\text{TURKEY}} = \frac{1.6 \times 10^{13}}{7.9 \times 10^{11}} \approx 2 \times 10^1 \approx 20 \times$

(use the back if you need more space)

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ACTIVATING PRIOR KNOWLEDGE:

We know what that magnitude can be used to determine the size of a number. Identify the magnitude of the following numbers:

32×10^{22}	45.2×10^3
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CLOSURE:

Gross Domestic Product (GDP) is an economic measurement used to show the market value of all the goods and services from a country. Below are the GDP figures for 8 countries for 2012 according to the United Nations. **Arrange them in order from greatest to least.**

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TEACHER NOTES:

Lesson should be fairly easy, Need to look at information on subatomic particles. Do students need to do the calculator information as stated in the lesson?