

NAME: _____

Math _____, Period _____

Mr. Rogove

Date: _____

LEARNING OBJECTIVE: We will simplify expressions that contain negative exponents. (G8M1L5)

CONCEPT DEVELOPMENT:

Recall the following exponent rules:

$x^m \cdot x^n = x^{m+n}$ multiplying

$(x^m)^n$ powers of powers

$(xy)^n = x^n y^n$ product of powers

$x^0 = 1$ zero exponent.

$8^{-3} = \frac{1}{8^3}$

Question: What should 7^{-2} mean? $\frac{1}{7^2}$

Definitions:

$x^{-n} = \frac{1}{x^n}$ $8^{-3} = \frac{1}{8^3}$

$x^{-n} = \frac{1}{x^n} = \frac{1}{\frac{1}{x^n}} = \frac{1}{1} \div \frac{1}{x^n} = \frac{1}{1} \cdot \frac{x^n}{1} = x^n$

Examples:

$5^{-2} = \frac{1}{5^2} = \frac{1}{25}$, $13^{-2} = \frac{1}{169}$, $2^{-4} = \frac{1}{2^4} = \frac{1}{16}$

Rewriting Numbers Using Negative Powers of 10

$\frac{1}{10^2}$ $\frac{1}{10^1}$ $10^0 = 1$
 $10^{-1} = 0.1$
 $10^{-2} = 0.01$
 $10^{-3} = 0.001$
 $10^{-4} = 0.0001$ $10^{-4} \cdot 10^4 = 1$

Example: $328.54 = (3 \times 10^2) + (2 \times 10^1) + (8 \times 10^0) + (5 \times 10^{-1}) + (4 \times 10^{-2})$

3 2 8 . 5 4

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GUIDED PRACTICE:

Write a simplified expression that is equivalent to the given one.

3×10^{-2} $3 \times \frac{1}{10^2}$ $3 \times \frac{1}{100} = \frac{3}{100} = 0.03$	2×10^{-4} $2 \times \frac{1}{10^4} = \frac{2}{10^4}$ $\frac{2}{10000} = \frac{1}{5000} = 0.0002$
<p>Write the expanded form in exponential notation:</p> <p>12:345</p> $(1 \times 10^1) + (2 \times 10^0) + (3 \times 10^{-1}) + (4 \times 10^{-2}) + (5 \times 10^{-3})$	<p>Write the expanded form in exponential notation:</p> <p>4.728</p> \checkmark
$x \cdot y^{-4}$ $x \cdot \frac{1}{y^4} = \frac{x}{y^4}$	$3 \cdot 4^{-7}$ $\frac{3}{4^7}$
$\frac{19^2}{19^5}$	$\frac{17^6}{17^{-3}}$ $\frac{17^6}{1} \cdot \frac{17^3}{1} = 17^9$ $\frac{17^6}{17^3} = 17^{6-3} = 17^3$

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<p style="text-align: center;">$(3xy)^{-2}$</p> $\frac{1}{(3xy)^2} = \frac{1}{3^2 x^2 y^2}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $\frac{1}{9x^2 y^2}$ </div> <p style="text-align: center;">↗</p>	<p style="text-align: center;">$(4g)^{-5}$</p>
<p style="text-align: center;">$(4x^3)^{-4}$</p>	<p style="text-align: center;">$(x^2 y^{-3})^{-8}$</p> $x^{(2 \cdot -8)} y^{(-3 \cdot -8)}$ $x^{-16} y^{24} = \frac{y^{24}}{x^{16}}$
<p style="text-align: center;">$\left(\frac{3}{4}\right)^{-4}$</p> $= \frac{1}{\frac{3^4}{4^4}} = \frac{1}{\frac{81}{256}}$ $= \frac{1}{1} \div \frac{81}{256} = \frac{1}{1} \cdot \frac{256}{81}$ <p style="text-align: center;">$(3 \div 4)^{-4}$</p> $3^{-4} \div 4^{-4} \quad \frac{1}{3^4} \div \frac{1}{4^4}$	<p style="text-align: center;">$\left(\frac{78}{5}\right)^{-5}$</p>

$$\frac{1}{3^4} \cdot \frac{4^4}{1} = \frac{4^4}{3^4}$$

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INDEPENDENT PRACTICE:

ab^{-1}	$\frac{4^0}{w^{-4}}$
$\frac{3x^{-4}}{y}$	$\frac{n^{-5}}{n^{-8}v^2}$
$\frac{6x^{-4}y^{-4}}{4x^{-7}}$	$\frac{8a^{-1}}{2c^{-3}}$
$(4s^3t^{-3}v^0)^{-6}$	$(2^{-3}d^{-3}f^4)^{-7}$

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ACTIVATING PRIOR KNOWLEDGE:

We know how to multiply and divide exponents in the context of having zero exponents

$4^0 \cdot 4^7 = 4^7 = 1$	$5^8 \div 5^8 = 5^0 = 1$
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CLOSURE:

Identify each of the following as either negative, between 0 and 1, or more than 1.

A. $-2^2 = -4$

B. $(-2)^2 = 4$

C. $2^{-2} = \frac{1}{4}$

D. $-2^3 = -8$

E. $(-2)^{-3} = \frac{1}{(-2)^3} = -\frac{1}{8}$

TEACHER NOTES:

Yummy Math: Negative Exponents-Ugh!