

**LEARNING OBJECTIVE:** We will look at constant rates using two variables and graph points related to constant rate problems. (G8M4L10)

**CONCEPT DEVELOPMENT:**

When we express a constant rate as a relationship between two variables, we can create **tables** to show the relationship and **graph** this relationship on a coordinate plane.

Example: Pauline mows a lawn at a constant rate. Suppose she mows 35 square feet in 2.5 minutes. How many square feet can she mow in  $x$  minutes?

**Equation in 2 variables:**

$$\frac{y}{x} = \frac{\text{area (sq. ft)}}{\text{time (min)}} \quad \star \left( \frac{y}{x} \right) = \left( \frac{35}{2.5} \right) x$$

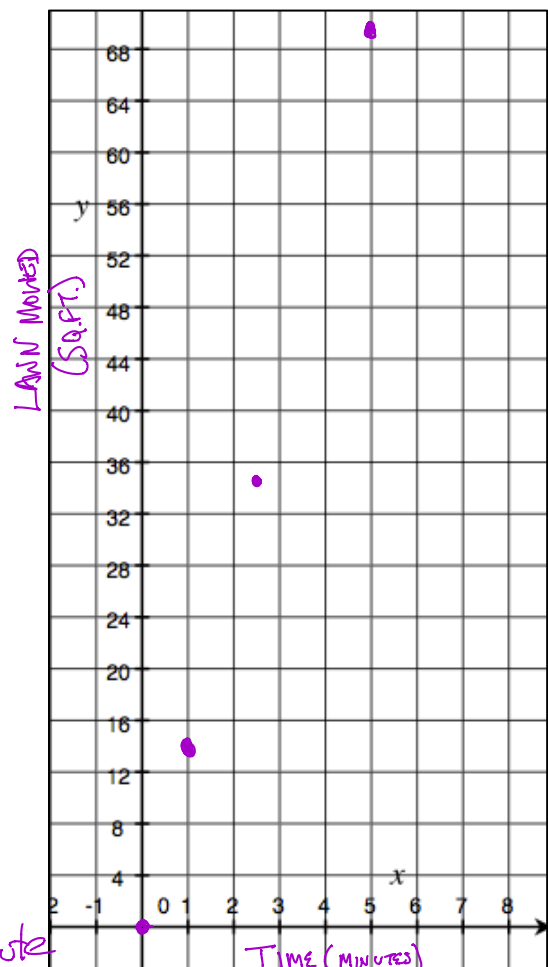
$$y = \frac{35}{2.5} x$$

$$y = 14x$$

**Graph:**

**Table:**

| Time (in minutes)<br>$x$ | Equation:<br>$y = 14x$ | Lawn mowed (in sq. feet) $y$ |
|--------------------------|------------------------|------------------------------|
| 2.5                      | $y = 14(2.5)$          | 35                           |
| 5                        | $y = 14(5)$            | 70                           |
| 10                       | $y = 14(10)$           | 140                          |
| 1                        | $y = 14(1)$            | 14                           |



> At 0 minutes, 0 lawn mowed

> Pauline mows 14 sq. ft in 1 minute

> Graph exist in Q1 only

**GUIDED PRACTICE:****Steps for Expressing Rates as Equations, Tables and in Graphs**

1. Begin by creating a linear equation using 2 variables that includes the rate.
2. Create a table and fill in the values.
3. Label and create a graph based on the table of values.

Water leaks out of a faucet at a constant rate. In 4 minutes, 35 milliliters of water dripped out. How many milliliters of water leak out in  $x$  minutes?

**Linear Equation (in two variables)**

$$\frac{y}{x} = \frac{\text{mL}}{\text{min}} \quad \frac{y}{x} = \frac{35}{4}$$

$$\frac{Hy}{x} = \frac{35x}{4}$$

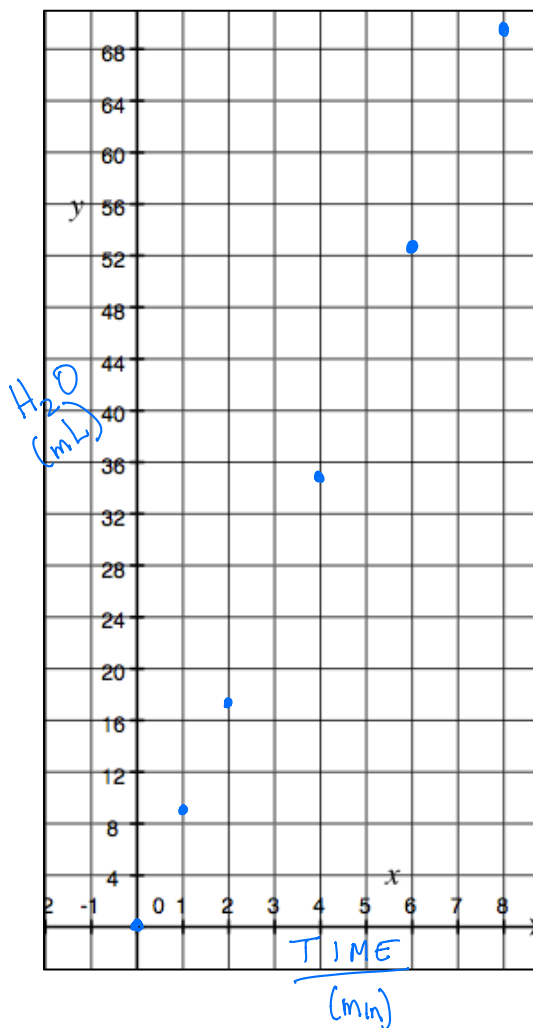
$$y = \frac{35}{4}x$$

$$y = 8.75x$$

The leak is 8.75 mL/min.

**Table of values**

| Time (in minutes) | Linear equation | Water (in mL) |
|-------------------|-----------------|---------------|
| $x$               | $y = 8.75x$     | $y$           |
| 1                 | $y = 8.75(1)$   | 8.75          |
| 2                 | $y = 8.75(2)$   | 17.50         |
| 4                 | $y = 8.75(4)$   | 35            |
| 6                 | $y = 8.75(6)$   | 52.50         |
| 8                 | $y = 8.75(8)$   | 70.           |



Kaia has a part time job as a babysitter. She worked last Friday evening and earned \$32.50 for working 2.5 hours. How much money would she earn in  $x$  hours?

### Linear Equation (in two variables)

$\frac{\text{dollars}}{\text{hrs.}}$

$$\frac{y}{x} = \frac{32.5}{2.5}$$

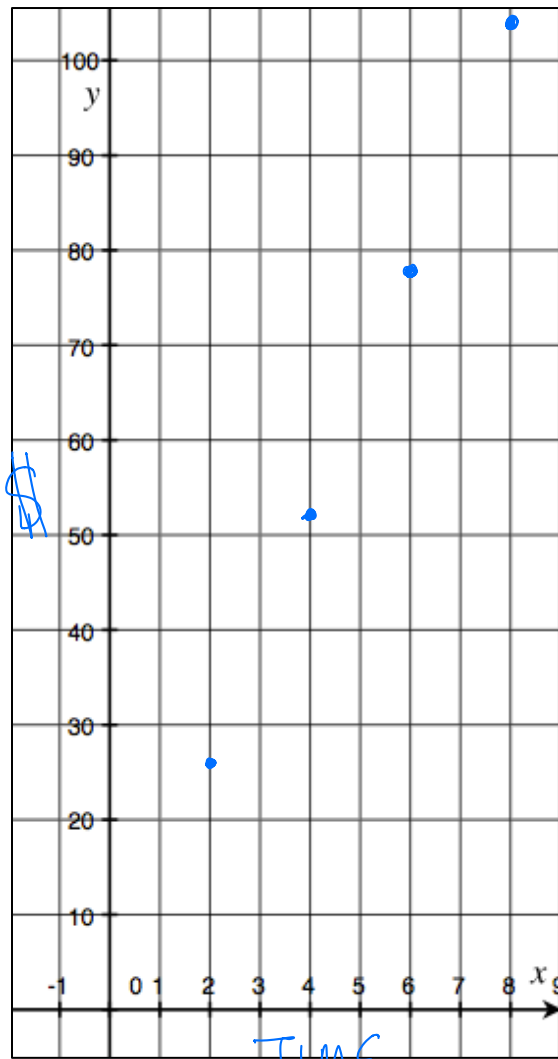
$$y = \frac{32.5}{2.5} x$$

$$y = 13x$$

Kaia gets paid \$13/hr.

### Table of values

| Time (in hours) | Linear Equation | Money earned (in dollars) |
|-----------------|-----------------|---------------------------|
| $x$             | $y = 13x$       | $y$                       |
| 2               | $y = 13(2)$     | 26                        |
| 4               | $y = 13(4)$     | 52                        |
| 6               | $y = 13(6)$     | 78                        |
| 8               | $y = 13(8)$     | 104                       |



Lucas types at a constant rate. He can type one full page of text in  $3\frac{1}{2}$  minutes. How many pages can type in  $x$  minutes?

### Linear Equation (in two variables)

$$\frac{\text{Pages}}{\text{minute}} = \frac{y}{x} = \frac{1}{3.5}$$

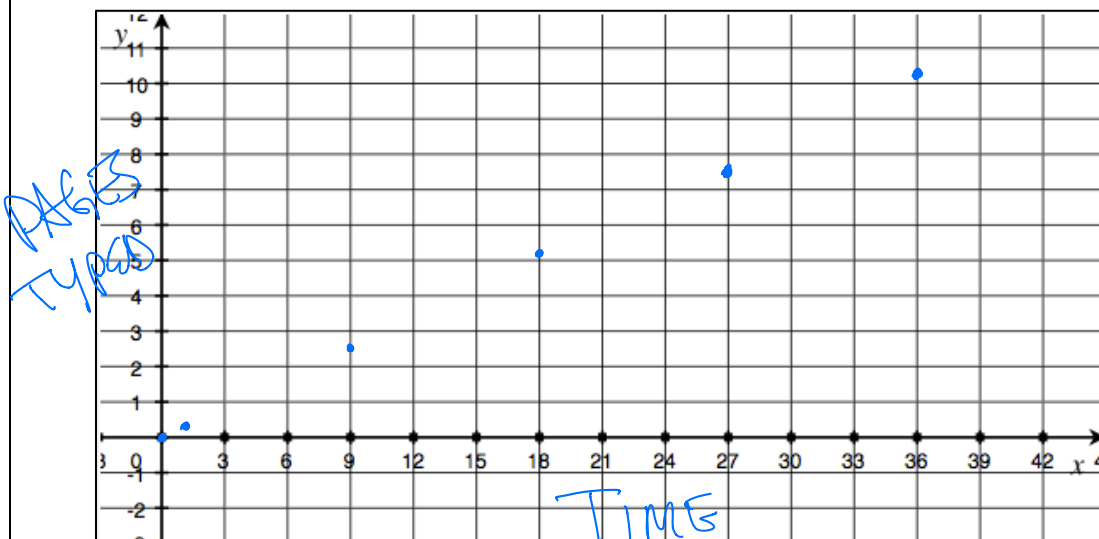
$$y = \frac{1}{3.5}x$$

$$y = \frac{2}{7}x$$

→ He types  $\frac{2}{7}$  of a page in 1 min

### Table of Values

| Time (in minutes)<br>$x$ | Linear Equation<br>$y = \frac{2}{7}x$ | Pages typed<br>$y$             |
|--------------------------|---------------------------------------|--------------------------------|
| 1                        | $y = \frac{2}{7}(1)$                  | $\frac{2}{7}$                  |
| 9                        | $y = \frac{2}{7}(9)$                  | $\frac{18}{7} = 2\frac{4}{7}$  |
| 18                       | $y = \frac{2}{7}(18)$                 | $\frac{36}{7} = 5\frac{1}{7}$  |
| 27                       | $y = \frac{2}{7}(27)$                 | $\frac{54}{7} = 7\frac{6}{7}$  |
| 36                       | $y = \frac{2}{7}(36)$                 | $\frac{72}{7} = 10\frac{2}{7}$ |



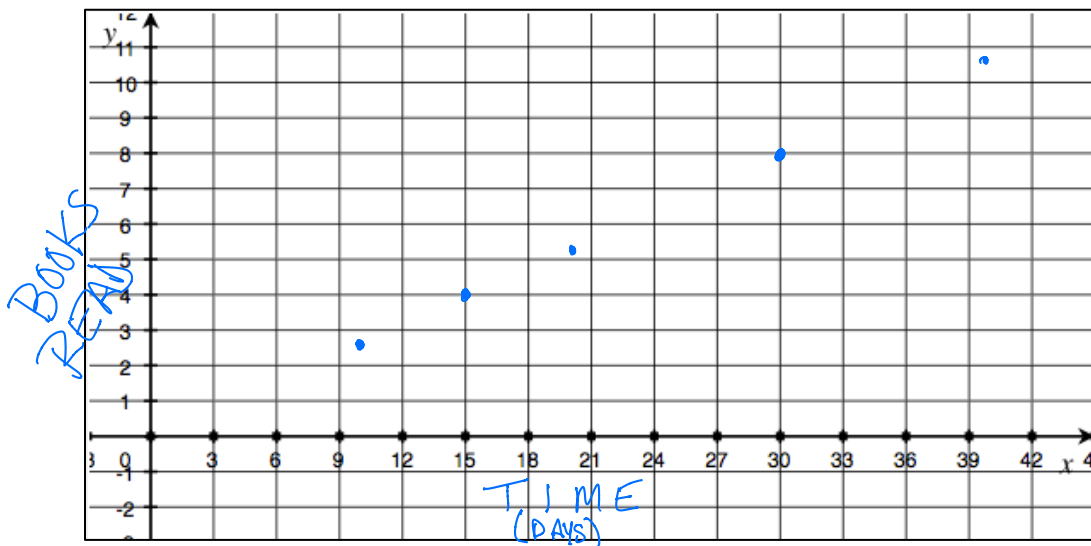
Rachel loves to read. She loves reading so much that she reads 4 books every 15 days. How many books can she read in  $x$  days?

### Linear Equation (in two variables)

$$y = \frac{4}{15}x$$

### Table of Values

| Time (in days) | Linear Equation     | Books read      |
|----------------|---------------------|-----------------|
| $x$            | $y = \frac{4}{15}x$ | $y$             |
| 10             |                     | $2\frac{2}{3}$  |
| 20             |                     | $5\frac{1}{3}$  |
| 30             |                     | 8               |
| 40             |                     | $10\frac{2}{3}$ |



NAME: \_\_\_\_\_

Math \_\_\_\_\_, Period \_\_\_\_\_

Mr. Rogove

Date: \_\_\_\_\_

**INDEPENDENT PRACTICE:**

**ACTIVATING PRIOR KNOWLEDGE:**

**CLOSURE:**

**TEACHER NOTES:**

Lesson 11 from ENY Module 4, Grade 8. Can also give the Yummy Math light bulbs activity as independent practice.

Homework is Lesson 11 problem set.