

**LEARNING OBJECTIVE:** We will work with proportional relationships in terms of average speed and constant speed. (G8M4L9)

**CONCEPT DEVELOPMENT:**

**Rates:** A proportional relationship between two quantities.

*Examples:* 3 coughs for 1 sneeze

- Six tacos cost \$7.50 at Taco Bell
- I can walk 3 miles in 48 minutes.
- My camera can take 10 pictures in 2 seconds. 10 cows in every sq. ft.
- I can text 120 words every 1.5 minutes.

*Non-Examples:*

- In a race, I spent 43 minutes on the first 4 miles, and 42 minutes on the last 3 miles.
- Each year, I grow 10% bigger than the year before.

Swim 5 laps in 10 minutes

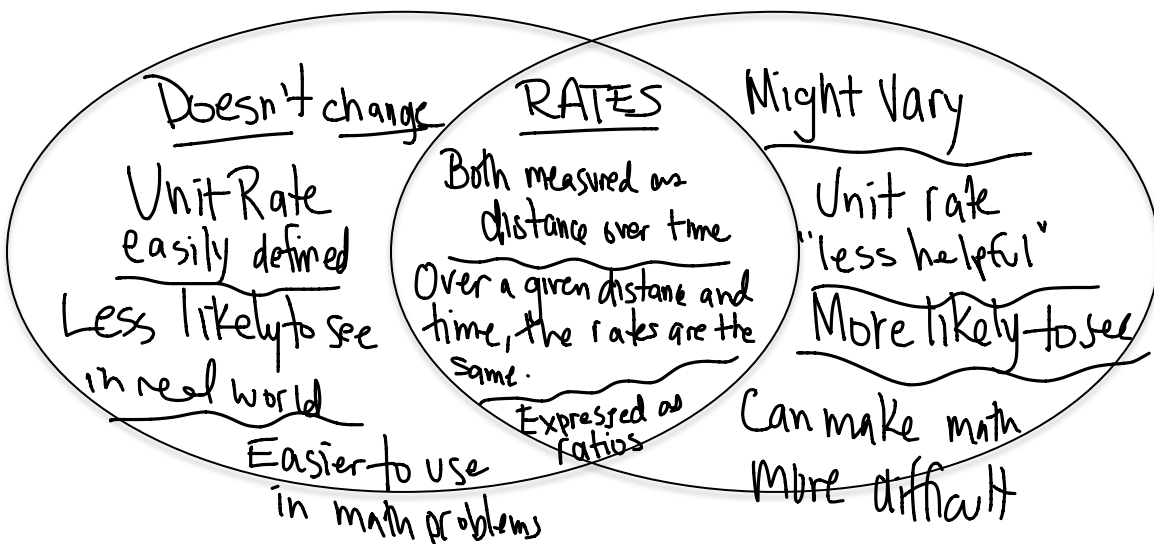
**We can express proportional relationships by creating tables.**

*Example:* If a 7<sup>th</sup> grader can write texts at a constant rate of 55 words per minute, we can create the following table:

Time (in minutes)	Words written in a text
$x$	$y$
1	55
2	110
3	165
4	220
10	550
100	5500

They can type  $y$  words in  $x$  minutes

**Constant Speed v. Average Speed**



$$\text{RATE} = \frac{\text{DISTANCE}}{\text{TIME}}$$

**GUIDED PRACTICE:****Steps to Representing Proportional Relationships in Two Variables**

1. Read the problem carefully and set up a rate that can help you measure the constant rate.
2. Let  $y$  represent the distance, cost, or other quantity (that is NOT time)
3. Let  $x$  represent the time.
4. Set up a proportion and solve for  $y$ .

Mason walks at a constant speed from his house to school 1.5 miles away. It took him 25 minutes to get to school.

How many miles has he walked after 15 minutes?

$$\frac{y}{x} = \frac{1.5}{25} \times \frac{y}{15}$$

$$1.5(15) = 25y$$

$$\frac{22.5}{25} = \frac{25y}{25}$$

$$0.9 = y$$

Mason walked  
0.9 miles in  
15 minutes

How many miles has he walked after  $x$  minutes?

$$\frac{\text{DIST}}{\text{TIME}} \left( \frac{y}{x} \right) = \left( \frac{1.5}{25} \right) x$$

$$y = \frac{1.5}{25} x \quad \text{UNIT RATE}$$

A plane travels at a constant rate from San Jose to Chicago 1,800 miles away. It takes 4.5 hours to get to Chicago.

How far had the plane gone after 2 hours?

$$\frac{1800}{4.5} \times \frac{y}{2}$$

$$\frac{4.5y}{4.5} = \frac{3600}{4.5}$$

$$y = 800$$

The plane travels  
800 miles in  
2 hours

How many miles has the plane traveled after  $x$  hours?

$$\frac{y}{x} = \frac{1800}{4.5}$$

$$\frac{y}{x} = 400$$

$$y = 400x$$

unit rate.

Mr. Rogove

Date: \_\_\_\_\_

Jennifer's car travels at a constant speed as she drives across country. It takes her 7 hours to travel 469 miles.

How many miles has she driven in 2.5 hours?

$$\frac{469}{7} \times \frac{y}{2.5}$$

$$7y = 1172.5$$

$$\frac{7y}{7} = \frac{1172.5}{7}$$

$$y = 167.5$$

Jennifer drove  
167.5 miles  
in 2.5 hrs

How many miles has she driven in  $x$  hours?

$$\frac{y}{x} = \frac{469}{7}$$

$$\frac{y}{x} = 67$$

$$y = 67x$$

Andrew rides the exercise bike at the gym at a constant speed. He is able to go 12 miles in 45 minutes.

How many <sup>miles</sup> would Andrew go if he was on the bike for 3.5 hours?

$$\frac{12}{45} \times \frac{y}{210}$$

$$\frac{45y}{45} = \frac{2520}{45}$$

$$y = 56$$

$$\frac{12}{.75} \times \frac{y}{3.5}$$

Andrew  
biked 56 miles  
in 3.5 hours

How many miles does Andrew bike in  $x$  hours?

$$\frac{y}{x} = \frac{12}{45}$$

$$y = \frac{12}{45}x$$

$$y = \frac{4}{15}x$$

$$y = \frac{4}{15}(16) \times y = 16x$$

Evan is 3 miles away from home. He rides on his skateboard further away from home at a constant speed. In 2 hours, he is able to skateboard 16 miles.

If Evan were to skateboard for 5 hours, how far away would he be from home?

$$\frac{16}{2} \times \frac{y-3}{5}$$

$$2(y-3) = 80$$

$$2y - 6 = 80$$

$$y = 43$$

Evan is 43 miles  
from home.

How far away from home would Evan be if he skateboarded for  $x$  hours?

$$\frac{y-3}{x} = \frac{16}{2}$$

$$x \left( \frac{y-3}{x} \right) = 8x$$

$$y-3 = 8x$$

$$y = 8x + 3$$

Joe flew in a plane 800 miles from his home to Denver. He got in a rental car and continued his journey away from his home at a constant rate. He was able to drive 360 miles in 8 hours.

How far away from home was Joe after he was driving for 3 hours?

How far away from home would Joe be after  $x$  hours in the car?

NAME: \_\_\_\_\_

Math \_\_\_\_\_, Period \_\_\_\_\_

Mr. Rogove

Date: \_\_\_\_\_

**INDEPENDENT PRACTICE:**

<p>Shannon is running around the track at a constant rate. She can run 4 laps in <math>5\frac{1}{2}</math> minutes.</p> <p>How long would it take her to run 6 laps?</p>          <p>How long does it take Shannon to run <math>x</math> laps?</p>	<p>Colby is swimming in a lake at a steady rate. He swims 900 yards in 21 minutes.</p> <p>How long does it take him to swim 500 yards?</p>          <p>How long would it take him to swim <math>x</math> yards?</p>
<p>Eric drives 25 miles from his home to a bike trail with his bike on the bike rack attached to his car. He then rides his bike further away from home at a constant rate. He rides his bike 162 miles in 9 hours.</p> <p>How far away from home is he after riding his bike for 5 hours?</p>          <p>How far away from home is Eric after riding his bike for <math>x</math> hours?</p>	<p>Create your own question here. Share it with the person you're sitting next to.</p>

NAME: \_\_\_\_\_

Math \_\_\_\_\_, Period \_\_\_\_\_

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Date: \_\_\_\_\_

**ACTIVATING PRIOR KNOWLEDGE:**

We remember how to calculate unit rates...

James can bike 25 miles in 3 hours. How many miles can he bike in one hour?	Chloe can text 190 words in 3 minutes. How many words can she text each minute?
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**CLOSURE:**

No closure??

**TEACHER NOTES:**

This might be a review lesson, or maybe not...first chance to introduce two variables. Maps to Module 4, Lesson 10 of ENY.

IM DVD Profits can be group practice problem and closure