

**LEARNING OBJECTIVE:** We will use equations to define and evaluate functions. (Lesson 96)

### ACTIVATING PRIOR KNOWLEDGE:

Study the different representations of a function below.

**TABLE:**

Input	0	1	2	3	4	5
Output	1	2	4	8	16	32

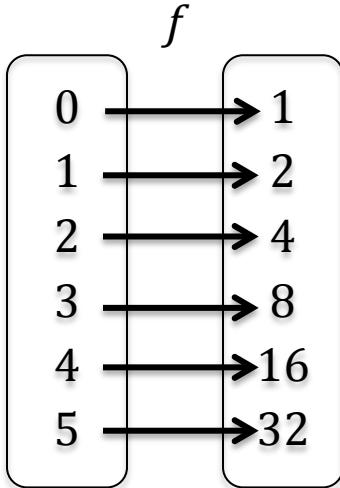
Exponential

**FUNCTION:**

Let  $f: \{0, 1, 2, 3, 4, 5\} \rightarrow \{1, 2, 4, 8, 16, 32\}$  such that  $x \mapsto 2^x$ .

- Outputs multiplying by 2
- Inputs adding 1
- Input/output relationship
- Inputs maps to the same output in each representation
- 2 is always base input is power
- They all represent the same equation  $y = 2^x$

**DIAGRAM:**



### CONCEPT DEVELOPMENT:

**Algebraic Function:** Given an algebraic expression in one variable, an algebraic function is a function  $f: X \rightarrow \mathbb{R}$  such that for each real number  $x$  in the domain  $X$ ,  $f(x)$  is the value found by substituting the number  $x$  into all instances of the variable symbol in the algebraic expression and evaluating.

Examples:

$$f(x) = x - 5$$

Domain: All real numbers

$$g(x) = 2^x$$

$$f(8) = 3$$

$$g(8) = 256$$

**GUIDED PRACTICE:****Steps to Evaluating Functions**

1. Read the function rule.
2. Substitute the appropriate  $x$  in  $X$  to the expression  $f(x)$ .
3. Evaluate the function.
4. Identify any restrictions on domain and range of the function as directed.

The squaring function is defined as follows:

Let  $f: X \rightarrow Y$  be the function such that  $x \mapsto x^2$ , where  $X$  is the set of all real numbers.

Find:

$$f(0) = 0^2 = 0$$

$$f(3) = 3^2 = 9$$

$$f(-2) = (-2)^2 = 4$$

$$f(\sqrt{3}) = (\sqrt{3})^2 = 3$$

$$f(-2.5) = (-2.5)^2 = 6.25$$

$$f\left(\frac{2}{3}\right) = \left(\frac{2}{3}\right)^2 = \frac{4}{9}$$

$$f(a) = a^2$$

$$f(a+3) = (a+3)^2 = a^2 + 6a + 9$$

Domain: All  $\mathbb{R}$

Range: All  $\mathbb{R} \geq 0$

The exponential function is defined as follows:

$$g(x) = 2^x$$

Find:

$$g(0) = 2^0 = 1$$

$$g(3) = 2^3 = 8$$

$$g(-2) = 2^{-2} = \frac{1}{4}$$

$$g(10) = 2^{10} = 1024$$

$$g\left(\frac{1}{2}\right) = 2^{\frac{1}{2}} = \sqrt{2}$$

Domain: All  $\mathbb{R}$

Range: All  $\mathbb{R}_{s \geq 0}$

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The square root function:

$$\text{Let } f(x) = \sqrt{x+2}$$

Find:

$$f(0) = \sqrt{0+2} = \sqrt{2}$$

$$f(-2) = \sqrt{-2+2} = \sqrt{0} = 0$$

$$f(7) = \sqrt{7+2} = \sqrt{9} = 3$$

$$f(14) = \sqrt{14+2} = \sqrt{16} = 4$$

$$f(5) = \sqrt{5+2} = \sqrt{7}$$

$$f(-5) = \sqrt{-5+2} = \sqrt{-3}$$

~~-5 is not a part of our domain!~~

$$f(4.25) = \sqrt{4.25+2} = \sqrt{6.25}$$

2.5

What are the restrictions on the domain and the range?

Domain: All  $\mathbb{R}$  where  $x \geq -2$ Range: All  $\mathbb{R}$  where  $y \geq 0$ Let  $f(x) = 4(3)^x$  Exponential

Find:

$$f(0) = 4(3)^0 = 4$$

$$f(1) = 4(3)^1 = 12$$

$$f(2) = 4(3)^2 = 36$$

$$f(3) = 4(3)^3 = 4 \cdot 27 = 108$$

$$f(4) - f(2) = 4 \cdot 3^4 - 4 \cdot 3^2$$

$$324 - 36 = 288$$

$$f(-3) = 4(3)^{-3} = \frac{4}{27}$$

What are the restrictions on the domain and range?

D: All  $\mathbb{R}$ R: All  $\mathbb{R}$   $x \geq 0$

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**INDEPENDENT PRACTICE:**

Students complete Problem Set for Independent Practice....Page s. 63-65 Rest is HW.

**CLOSURE:**

Write three different polynomial functions such that  $f(3) = 2$

$$f(x) = \frac{6}{x}, f(x) = \frac{2}{3}x, f(x) = x^2 - 2x - 1$$

**NOTES:**  $f(x) = x - 1$        $f(x) = -x^2 + 11$

This accompanies lesson 10 from Alg 1 Mod 3.

$$f(x) = 2, f(x) = x^2 - 7$$